

# *Simulating the Dynamic Macroeconomic and Microeconomic Effects of the FairTax<sup>1</sup>*

***Abstract** - America's aging coupled with high and growing old-age health and pension benefits augers for much higher payroll taxes, with damaging effects on the U.S. economy. This prognosis is supported by our analysis of a detailed dynamic life-cycle general equilibrium model. The FairTax, which proposes to replace the federal payroll, personal income, corporate income, and estate tax with a progressive consumption tax, offers a potential alternative to this dismal economic future. According to our simulation model, these policy changes would lead to major improvements in the U.S. capital stock, long-run real wages and the well-being of the majority of Americans.*

## INTRODUCTION

This paper uses a life-cycle general equilibrium model developed in Fehr, Halder, Jokisch, and Kotlikoff (2003), Fehr, Jokisch, and Kotlikoff (2004a, 2004b, 2005a, 2005b) and Jokisch (2006) to study the dynamic macroeconomic and microeconomic effects of replacing all federal taxes with a progressive, broad-based consumption tax, namely the FairTax. The FairTax combines a federal retail sales tax, levied at a single rate, with a rebate the size of which depends on the household's characteristics. Businesses would be exempt from the FairTax on their purchases, since such purchases do not represent consumption. The FairTax also increases Social Security benefits to maintain their real purchasing power. Finally, the FairTax reduces non-Social Security federal expenditures to help pay for its introduction of a major new transfer (equivalently, tax expenditure), namely the FairTax rebate.

As specified in HR25, the legislation that would implement the FairTax, the FairTax would be levied at a 30 percent nominal rate and a 23 percent effective rate. The nominal rate refers to the rate one would pay at the store in purchasing a good or service. To see the relationship between the nominal and effective rates, consider spending one dollar at a retail store. With a 30 percent sales tax rate, one ends up with only 77 cents in actual consumption, since 23 cents (which is 30 percent of 77 cents) goes to taxes. So paying a 30 percent retail

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<sup>1</sup> Part of this paper draws directly on Fehr, Jokisch, and Kotlikoff (2005b).

sales tax when one spends one's income or wealth is the same as facing no retail sales tax, but having one's income and wealth reduced by 23 percent.

Households finance current and future consumption with their current wealth and their current and future labor earnings. Taxing consumption expenditures is, thus, effectively equivalent to taxing what is used to pay for consumption, namely existing wealth as well as today's and tomorrow's labor income. In the case of the FairTax, every dollar of existing wealth as well as every dollar of current and future earnings would be effectively taxed at a 23 percent rate.

Under the current U.S. federal tax system, total effective marginal tax rates on labor supply are higher than 23 percent for almost all American households. Indeed, as shown in Kotlikoff and Rapson (2005), typical middle-aged and middle-income earners face total effective federal marginal tax rates on working of roughly 30 percent. For these and most other households, the FairTax would dramatically improve labor supply incentives.

Since the FairTax taxes consumption at the same rate no matter when it occurs, it imparts no incentive to consume now as opposed to later and, thus, no disincentive to save. In economic terms, the FairTax's marginal effective tax rate on saving is zero. In contrast, the existing federal tax system imposes very high marginal effective tax rates on saving. This point is also documented in Kotlikoff and Rapson (2005), who report marginal taxes on saving for stylized households ranging from 20 percent to 54 percent.

In addition to imposing, in almost all cases, much lower marginal taxes on working and, in all cases, dramatically lower marginal taxes on saving, the FairTax imposes lower average taxes on low- and middle-income working households than does the current system. It does so, in part, by broadening the tax base from what is now primarily labor income to the

sum of labor income and current wealth and, in part, by reducing non-Social Security real federal expenditures to help pay for the FairTax rebate. In particular, the reform implies a real reduction in federal purchases of goods and services, which many Americans may view as desirable. In this regard, it should be noted that federal purchases of goods and services, measured as a share of GDP, have risen by over one-fifth since 2000.

Would switching to the FairTax enhance or undermine progressivity? The implicit taxation of wealth under the FairTax is certainly a highly progressive element of the proposed reform. So too is the elimination of the highly regressive payroll (Federal Insurance Contributions Act, or FICA) tax and the implementation of the FairTax's highly progressive rebate. On the other hand, the personal income tax is progressive, albeit less progressive than many seem to believe (see Gokhale, Kotlikoff, and Sluchynsky (2002)). Understanding the FairTax's net impact on progressivity is one of this study's goals. What about the FairTax's treatment of the elderly? Well, HR25 would increase Social Security benefits by 30 percent to maintain the purchasing power of those transfer payments. In addition, it provides the rebate to all American households, including the elderly. In so doing, it overcompensates the poor elderly who live either entirely or primarily off of Social Security; i.e., the poor elderly receive the rebate even though the purchasing power of their Social Security benefits remains unchanged.

In contrast to the poor elderly, the middle class and rich elderly finance much or most of their consumption from their accumulated wealth. The purchasing power of this wealth is reduced by the FairTax. Hence, the FairTax imposes a higher fiscal burden on the middle-class elderly and the rich elderly than does the existing tax structure. In the life-cycle model, the elderly have a higher propen-

sity to consume out of their remaining lifetime resources than do young and certainly future generations. Hence, shifting the burden of taxation from young and future generations to initial older generations reduces aggregate private consumption and increases national investment. Increased investment means, in turn, more capital per worker and, thus, higher labor productivity and real wages.

A key question about the FairTax is its real revenue neutral rate, i.e., the rate needed to preserve real spending by both federal and state governments. Gale (2005) suggests that the FairTax's proposed 23 percent effective (tax inclusive) rate would fall significantly short of achieving real revenue neutrality. Bachman, Haughton, Kotlikoff, Sanchez-Penalver, and Tuerck (2006) conclude the opposite. Although we find Bachman et al. (2006) persuasive, our highly stylized model is not the U.S. economy. Sustaining a 23 percent rate in our model requires an 18 percent cut in federal discretionary spending as a share of national income. Alternatively, maintaining real discretionary spending levels in switching to the FairTax requires a 26 percent effective rate. Since the FairTax proposal specifies a 23 percent effective rate and no cuts in discretionary spending, we simulate two alternative policies. The first is implementing the FairTax at a 23 percent rate, but cutting discretionary spending by 18 percent. The second is maintaining discretionary spending as a share of national income, but implementing the FairTax at a 26 percent effective rate.

The two alternative simulations yield very similar results. Relative to maintaining the current pay-as-you-go policy of financing entitlements, either manner of switching to the FairTax will precipitate a very major increase in the U.S. capital stock and real wages over the course of the century, prevent what would otherwise be a doubling to the highly regressive payroll tax, and effect very major welfare gains, particularly for the poorest current

and future members of society. Indeed, once one moves to generations postdating the baby boomers, there are positive welfare gains for all income groups in each cohort.

Take, for example, the policy of shifting to a 23 percent FairTax rate and cutting the scale of discretionary real spending by 18 percent. This policy raises marginal labor productivity and real wages, over the course of the century, by 25.0 percent and long-run output by 16.1 percent. It also reduces by half the long-run increase in the effective rate of wage taxation needed to pay the Social Security and healthcare benefits of an aged country. These macroeconomic gains have important microeconomic welfare implications. In the long run, low-income households experience a 26.3 percent welfare gain, middle-income households experience a 12.4 percent welfare gain, and high-income households experience a 5.0 percent welfare gain. This is a very progressive long-run outcome. But progressivity marks the entire transition. Low-income households who are initially alive at the time of the reform, whether they are young, middle age, or old, all experience welfare gains ranging from 4.7 percent to over 20 percent. Who pays for these substantial welfare gains? The answer is hardly anyone. The initial rich elderly and middle aged as well as some middle-age middle-income households are made worse off, but their welfare losses are quite small compared to the welfare gains experienced by the current poor and future generations. One reason the FairTax offers such significant welfare improvements for winners and such small losses for losers is that it significantly improves economic incentives, particularly the incentive to save, and, thereby, reduces economic distortions, i.e., excess burden.

The remarkable point here is the size of the gains from the reform relative to the losses. Yes, some initial high- and middle-income households are made

worse off, but their welfare losses are minor compared with the gains available to future generations, particularly the poorest members of future generations. The economic and welfare gains from switching to the FairTax are somewhat smaller if one models the U.S. economy as fully open to international capital flows. But the gains are, nonetheless, large and very significant. Moreover, a very similar pattern of macroeconomic, microeconomic, and welfare changes arises under our alternative policy in which we peg the level of real spending relative to the economy and implement the FairTax at an initial 26 percent rate.

While our model is highly stylized and ignores political economy issues examined by Krussell, Quadri, and Ríos-Rull (1996) and others, it suggests that the FairTax offers a real opportunity to improve the U.S. economy's performance and the well-being of the vast majority of Americans. The winners from this reform, primarily those who are least well off, experience very major gains, and the losers experience only minor losses.

Having said this, we hasten to raise a caveat informed by the important work of Nishiyama and Smetters (2005). These authors stress the advantage of the current progressive income tax system in pooling idiosyncratic income risk across and within generations. But their study compares a progressive income tax with a proportional consumption tax, whereas the FairTax represents a progressive consumption tax thanks to its highly progressive rebate. An important area of future research would be to simulate the FairTax in the context of the idiosyncratic shocks assumed by Nishiyama and Smetters (2005).

The model generating the above-mentioned results treats the U.S. economy as closed, which in this context means its domestic investment is determined by its own saving. As shown by Feldstein and Horioka (1980), there is much truth to this proposition. However, newer

studies like, e.g., Mc Morrow and Roeger (2004) show that international capital market integration increased during the last decades raising the importance of international capital flows in domestic investment. We, therefore, also consider the other extreme assumption, namely that U.S. domestic investment is fully determined by international capital flows, i.e., we also run the model treating the U.S. as a small open economy. Our small open economy results are not quite as dramatic as our closed economy findings. But the potential economic gains remain impressive and run in the same direction. In this case, the shift to the FairTax raises the long-run (year 2100) capital stock by 43.0 percent and long-run real wages by 15.3 percent. In the long run, low-income households experience a 21.4 percent welfare gain, middle-income households experience a 9.6 percent welfare gain, and high-income households experience a 4.7 percent welfare gain.

## OUR MODEL AND ITS PREDECESSORS

The usefulness of our findings depends, of course, on the realism of our model. Our model includes age- and year-specific fertility and mortality rates; lifespan uncertainty; age- and year-specific pension, disability, health care, and other government transfer policies; year-specific government purchases of goods and services; government debt; high, middle, and low earners within each cohort; personal income taxes, corporate income taxes, and payroll taxes; technological change; age-specific inheritances; age-specific and unintended bequests; intertemporally separable CES (constant elasticity of substitution) utility functions in consumption and leisure; Cobb-Douglas production functions; the presence of children's utility in parents' utility functions when the children are young; exogenously specified age-, earnings-class-, and year-specific

immigration; and cohort-specific time preference rates.

The development of dynamic life-cycle simulation models was stimulated by Feldstein's (1974) article contending that government pension systems lower national saving. Early dynamic analysis of government pension programs and other policies include Kotlikoff (1979), Summers (1981), Auerbach and Kotlikoff (1983, 1987), and Seidman (1986). More recent papers have considered the importance of land, earnings uncertainty, political economy considerations, liquidity constraints, different options for funding Social Security, and human capital decisions. These studies include Hubbard and Judd (1987), İmrohoroğlu, İmrohoroğlu, and Joines (1995, 1999), Kotlikoff (1996), Huang, İmrohoroğlu, and Sargent (1997), Huggett and Ventura (1999), Cooley and Soares (1999a,b), De Nardi, İmrohoroğlu, and Sargent (1999), Kotlikoff, Smetters, and Walliser (1998a,b, 1999, 2002), Raffelhüschen (1989, 1993), Heckman, Lochner, and Taber (1998), Bohn (2001), Smetters and Walliser (2004), Nishiyama and Smetters (2005), and Fehr and Habermann (2005).

This model, like our previous ones, builds on Auerbach and Kotlikoff's (1987) overlapping generation (OLG) model. Auerbach and Kotlikoff also simulated demographic transitions, but their model assumed that all agents gave birth at a fixed age, died and bequeathed at a fixed age, and received inheritances at a fixed age. Kotlikoff, Smetters, and Walliser (2001) advanced the Auerbach-Kotlikoff model by incorporating age-specific fertility and inheritance, lifespan extension, intragenerational earnings heterogeneity, and additional fiscal institutions. Fehr, Jokisch, and Kotlikoff (2004a,b, 2005a,b) included lifespan uncertainty as well as bequests arising from incomplete annuitization. They also introduced multiple regions with international capital mobility and immigration.

As in Kotlikoff, Smetters, and Walliser (2001), our model features monozygotic reproduction with agents in their child-bearing years giving birth each year to fractions of children. This means of finessing marriage and family formation permits us to incorporate changes through time in age-specific fertility rates and to closely line up our model's age-specific population shares to those forecast for the four regions.

We assume that agents care about their children's utility when they are young and, as a consequence, make consumption expenditures on behalf of their children (pay for their consumption), but only when the children are young. We also assume that agents die with realistic mortality probabilities starting at age 68. Agents fully appreciate the uncertainty of their longevities and maximize, at any point in time, their expected remaining lifetime utilities. The inclusion of lifespan uncertainty permits a realistic modeling of bequests and inheritances.

We generate bequests by assuming that agents fail to annuitize their assets in old age. Hence, when they die, they leave undesired bequests to their children. Since agents die at different ages and have children of different ages, their heirs also inherit at different ages. Agents who were born when their parents were young receive inheritances later in their life than do their younger siblings. Finally, uninsurable lifespan uncertainty leads agents to gradually reduce their consumption in old age.

A final, but very important, feature of our framework is its intra-cohort disaggregation. As in Kotlikoff, Smetters and Walliser (2001), we consider three income classes within each generation, each with its own earnings ability. Immigrants are also split into these income classes, permitting us to simulate the arrival of immigrants with different stocks of human and physical capital. The following sections present the general structure of our model.

A more detailed description of the model (within a multi-country framework) is provided in Fehr et al. (2003) and Jokisch (2006).

*Demographics*

Our model is populated by households who live at most to age 90. Consequently, there are 91 generations with surviving members at any point in time. The individual life cycle of a representative agent is described in Figure 1. Between ages 0 and 20, our agents are children who earn no money and are supported by their parents. At age 21, our agents leave their parents and go to work. Between ages 23 and 45, our agents give birth to fractions of children at the beginning of each year, i.e., the first (fraction of) children are born when the agents are 23 and the last are born when they are age 45. An agent's first-born children (fractions of children) leave home when the parents are age 43, while the last-born leave when the agents are age 66. Our agents die between ages 68 and 90. The probability of death is one at age 91. Children always outlive their parents, meaning that parents always outlive grandparents. To see this, note that if a parent reaches age 90, his or her oldest children will be 67. These are children who were born when the parent was age 23.

In each year new immigrants in each skill and age group arrive with the same number and age distribution of children and the same level of assets as natives of the identical skill and age. Once they

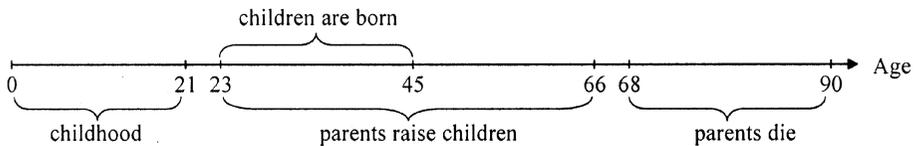
arrive, they act just like native Americans in terms of their labor supply and consumption choices. To specify the current and future demographic structure, we start with year-2000<sup>2</sup> age-specific population [ $\bar{N}(a,2000)$ ] and age-specific net-immigration [ $\bar{N}\bar{M}(a,2000)$ ] counts where  $a$  indicates age.

In constructing existing as well as future age-population counts, we have to link each initial cohort between the ages of 0 and 67 to those of their parents who are still alive. The reason is that children receive bequests from their parents, and the levels and timing of these inheritances depend on the ages of their parents. This linkage is achieved by applying past fertility rates to each cohort under age 68 in year 2000. If, for example, 15 percent of the parents of newborns in 1980 were 25 years old, then 15 percent of the 20-year-olds in year 2000 are assigned to parents age 45.

In addition, each cohort is split into three income classes  $k$ . Specifically, we assume that 35 percent of each cohort belong to the lowest income class, ten percent, to the top income class, and the remaining 55 percent, to the middle income class. We denote the population vector for year  $t$  as  $N(a,t,s,k)$  where  $a = 1, \dots, s = 23, \dots, 45, k = 1,2,3$ . The term  $s$  references the age of the parent at the time of birth of agents age  $a$  in 2000.

To determine the evolution of the population in each region over time, we applied region-, age-, and year-specific mortality and fertility rates to the cohorts alive in year 2000 as well as to their children as they reach

Figure 1. The Individual Life Cycle



<sup>2</sup> Although the economic model starts in year 2004, we chose year 2000 as the initial year for the population projections due to better data availability.

their ages of fertility and mortality. In the baseline path, the exogenous current and future mortality and fertility rates follow the medium variant of the United Nations population projection (UNPD, 2003).

According to this projection, U.S. life expectancy at birth rises by 4.5 years between 2000 and 2050. Table 1 shows our model's life expectancies at birth through 2050. After 2050, mortality rates as well as the number of newborns are kept constant to ensure the model eventually attains a steady state. The model's life expectancies at birth are higher than the official projections. But this is to be expected given that our model's agents do not die prior to age 68. However, the model's life expectancies conditional on reaching age 60 are close to those reported by the UNPD (2005).

As indicated in Table 1, the model replicates very closely the time path of the official prediction of the U.S. total fertility rate through 2050, after which we adjust the fertility rate to ensure that fertility plus net immigration, set at one million net immigrants per year, just reproduce the U.S. population, i.e., achieve zero population growth.

Given the population age structure in year 2000 as well as projected future

fertility, mortality, and net immigration rates, we compute the population vector  $N(a,t,s,k)$  for the years  $t$  between 2001 and 2050. After year 2050, fertility rates are endogenously adjusted in order to achieve zero population growth and a stable population age structure. Since net immigration is positive in the U.S., the population-stabilizing post-2050 fertility rates are below 2.0.

Table 1 also shows projected changes over time in total populations and population age structures. Due to high fertility and net immigration rates, the U.S. population is projected to increase from 275 million in 2000 to 442 million in 2100. As the table makes clear, the model's demographic machinery does a remarkably good job matching official projections with respect to the absolute number and age compositions of their respective populations. We now describe this machinery in more detail.

The total number of children of an agent age  $a$  in income class  $k$  in year  $t$  is recorded by the following function:

$$[1] \quad KID(a,t,k) = \sum_{j=u}^m \frac{N(j,t,a-j,k)}{\sum_{s=23}^{45} N(a,t,s,k)}$$

$23 \leq a \leq 65, k = 1,2,3,$

**TABLE 1**  
COMPARING ACTUAL AND SIMULATED POPULATION PROJECTIONS

Year	2000	2010	2020	2030	2040	2050	2100
<b>Fertility Rate</b>							
Model	2.11	2.05	2.00	1.95	1.90	1.85	1.77
Official <sup>a</sup>	2.11	2.08	2.03	1.95	1.89	1.85	-
<b>Life Expectancy at Birth</b>							
Model	81.7	82.1	82.5	83.0	83.4	83.8	83.8
Official <sup>a</sup>	77.1	78.3	79.1	79.9	81.0	81.6	-
<b>Total Population (in mio.)</b>							
Model	276.2	307.3	340.0	366.4	385.8	400.3	442.0
Official <sup>a</sup>	285.0	314.9	344.3	370.4	391.4	408.7	-
<b>Age Structure</b>							
<15	Model	21.6	20.1	19.7	18.5	17.8	15.9
	Official <sup>a</sup>	21.8	20.5	20.0	19.3	18.5	-
15-64	Model	66.2	67.2	64.0	61.4	61.7	60.7
	Official <sup>a</sup>	65.9	66.6	64.1	61.5	61.7	-
65-90	Model	12.2	12.7	16.3	20.1	20.2	23.3
	Official <sup>a</sup>	12.3	12.8	15.9	19.2	19.8	-

<sup>a</sup>United Nations Population Division (2003), Medium Variant Projections.

where  $u = \max(0; a - 45)$  and  $m = \min(20; a - 23)$ . Recall that agents younger than 23 have no children and those over 65 have only adult children, i.e.,  $KID(a, t, k) = 0$  for  $0 \leq a \leq 22$  and  $66 \leq a \leq 90$ . Agents between these ages have children. Take, for example, a 30-year-old agent. Such an agent has children who were born in the years  $(a - j)$  since she/he was 23. In year  $t$ , these children are between age  $0 \leq j \leq 7$ . The  $KID$ -function [1] sums the total number of kids of the respective parent-income class generation and divides it by the total number of parents of age  $a$  in year  $t$  who belong to income class  $k$ . This function takes into account that the family's age structure will change over time due to changing fertility. This approach permits the distribution of births by the ages of parents to change over time—an important improvement relative to the birthing process stipulated in Kotlikoff, Smetters and Walliser (2001).

*The Household Sector*

As previously mentioned, we do not distinguish between natives and immigrants once the immigrants have joined the native earnings- and age-specific cohorts. The model's preference structure is represented by a time-separable, nested, CES utility function. Remaining lifetime utility  $U(j, t, s, k)$  of a generation of age  $j$  at time  $t$  whose parents were age  $s$  at time of birth and who belongs to income class  $k$  takes the form

$$[2] \quad U(j, t, s, k) = V(j, t, s, k) + H(j, t, s, k),$$

where  $V(j, t, s, k)$  records the agent's utility from her/his own goods and leisure consumption, and  $H(j, t, s, k)$  denotes the agent's utility from the consumption of her/his children.<sup>3</sup> The two sub-utility functions are defined as follows:

$$[3] \quad V(j, t, s, k) = \frac{1}{1 - \frac{1}{\gamma}} \sum_{a=j}^{90} \left( \frac{1}{1 + \theta} \right)^{a-j}.$$

$$P(a, i) \left[ c(a, i, s, k)^{1 - \frac{1}{\rho}} + \alpha \ell(a, i, s, k)^{1 - \frac{1}{\rho}} \right]^{1 - \frac{\gamma}{\rho}}$$

and,

$$[4] \quad H(j, t, s, k) = \frac{1}{1 - \frac{1}{\gamma}} \sum_{a=j}^{90} \left( \frac{1}{1 + \theta} \right)^{a-j}.$$

$$P(a, i) KID(a, i, k) c_k(a, i, s, k)^{1 - \frac{1}{\gamma}}$$

where  $c(a, i, s, k)$  and  $\ell(a, i, s, k)$  denote consumption and leisure, respectively, and  $i$  is defined as  $i = t + a - j$ . The children's consumption of income class  $k$  parents who are age  $a$  in period  $i$  and whose parents were age  $s$  at the time of their birth is defined as  $c_k(a, i, s, k)$ . Note that the number of children is independent of the grandparent's age at the time of the birth of the parents.

Since lifespan is uncertain, the utility of consumption in future periods is weighted by the survival probability of reaching age  $a$  in year  $i$ ,

$$[5] \quad P(a, i) = \prod_{u=j}^a [1 - d(u, u - a + i)],$$

which is determined by multiplying the conditional survival probabilities from year  $t$  (when the agent's age is  $j$ ) up to year  $i$ . Note that  $d(j, t)$  is the mortality probability of an agent age  $j$  in year  $t$ . The parameters  $\theta$ ,  $\rho$ ,  $\alpha$ , and  $\gamma$  represent the "pure" rate of time preference, the intratemporal elasticity of substitution between consumption and leisure at each age  $a$ , the leisure preference parameter, and the intertemporal elasticity of substitution between consumption and leisure in different years, respectively.

<sup>3</sup> We only consider the utility of adults (including their utility for their children) in the welfare analysis and do not take into account the agent's utility in her/his own childhood.

In maximizing utility, agents choose their demand for leisure subject to the constraint that leisure in each period not exceed one, which is the time endowment. The determination of the shadow values of these leisure constraints, when these constraints are binding, is included as part of the maximization. To ensure that agents retire by a designated maximum retirement age, we set the net wage at that age and thereafter to zero.

Given the asset endowment  $a(j, t, s, k)$  of the agent in year  $t$ , maximization of [2] is subject to a lifetime budget constraint defined by the sequence:

$$\begin{aligned}
 [6] \quad a(j+1, t+1, s, k) = & [a(j, t, s, k) \\
 & + I(j, t, s, k)](1+r(t)) \\
 & + w(t)E(j, k)[h(j, t) - \ell(j, t, s, k)] \\
 & - T(j, t, s, k) - c(j, t, s, k) \\
 & - \Psi KID(j, t, k)c_k(j, t, s, k),
 \end{aligned}$$

where  $\Psi$  is the conventional equivalent scale of consumption of kids,  $r(t)$  is the pre-tax return on savings, and  $I(j, t, s, k)$  denotes the inheritance the agent receives in year  $t$ . When the parents die between age 68 and 90, their remaining assets are split between their children. Consequently, inheritances of agents who are age  $j$  in year  $t$  and whose parents were age  $s$  at their birth are defined by

$$[7] \quad I(j, t, s, k) = \frac{d(j+s)\bar{A}(j+s, t, k)}{\sum_{u=23}^{45} N(j+s-u, t, u, k)}.$$

The numerator defines the aggregate assets of income class  $k$  parents who die in year  $t$  at age  $j+s$ . The denominator defines these parents' total number of

children who are between ages  $j+s-45$  and  $j+s-23$  in year  $t$ . The receipt of inheritances requires us to distinguish members of each cohort according to the ages of their parents at birth. The parents' ages at death determine when the children receive their inheritances. While the oldest children (born when their parents are age 23) receive their inheritances between ages 45 and 67, the youngest children (born when their parents are age 45) receive their inheritances earlier in life, between ages 23 and 45.

As in Altig, Auerbach, Kotlikoff, Smetters, and Walliser (2001) and Kotlikoff, Smetters and Walliser (2001), we assume that technical progress causes the time endowment  $h(\cdot)$  of each successive generation to grow at the rate  $\lambda$ , i.e.,

$$[8] \quad h(a, i) = (1+\lambda)h(a, i-1).$$

The proposition here is not that time, per se, expands for successive generations, but rather that each successive generation is more effective in using time to either perform work or enjoy leisure. Treating technical change in this manner is essential to ensure that the economy achieves a long-run steady state.<sup>4</sup> The assumption of labor-augmenting technical change would not, for example, be compatible with a long-run steady state given the nature of the model's preferences. And having the economy achieve a long-run steady state provides, in effect, the terminal conditions needed by our algorithm to solve for the model's equilibrium transition path.<sup>5</sup>

Gross labor income of the agent in year  $t$  is derived as the product of her/his labor supply and her/his wage rate. The latter is the product of the gross wage rate  $w(t)$  in period  $t$  and the age- and class-specific earnings ability:

<sup>4</sup> Note that the assumed exogenous productivity growth is isomorphic to a higher rate of population growth.

<sup>5</sup> For a very detailed discussion of the implementation of technical progress in OLG models of the Auerbach-Kotlikoff type, see Jokisch (2006).

$$[9] \quad E(a, k) = \xi(k)e^{4.47+0.033(a-20)-0.00067(a-20)^2} \cdot (1 + \lambda)^{a-21}$$

with

$$\xi(1) = 0.2, \xi(2) = 1.0, \xi(3) = 5.0.$$

The middle-income class profile is taken from Auerbach and Kotlikoff (1987). The shift parameters  $\xi(k)$  are then applied to derive income-class-specific profiles. Moreover, since technological change is an important determinant of secular growth over the life cycle, we multiply the age-specific longitudinal earnings ability profile by the term involving  $\lambda$ . Hence, the longitudinal age-wage profile is steeper the larger is the rate of technological change.

The net taxes  $T(j, t, s, k)$  of an agent in year  $t$  are defined as

$$[10] \quad T(j, t, s, k) = \tau^c(t)[c(j, t, s, k) + \Psi KID(j, t, k)c_K(j, t, s, k) + \tau^r(t)r(t)[a(j, t, s, k) + I(j, t, s, k)] + \bar{\tau}^w(j, t, s, k)W(j, t, s, k) + [\bar{\tau}^p(j, t, s, k) + \bar{\tau}^h(j, t, s, k) + \bar{\tau}^d(j, t, s, k)]W(j, t, s, k) - Pen(j, t, s, k) - di,$$

where  $\tau^c(t)$  is the consumption and  $\tau^r(t)$  the capital income tax rate. Wage taxes as well as social security contributions are progressive. The (individual) average wage tax rate is denoted as  $\bar{\tau}^w(j, t, s, k)$ . Due to our assumed ceiling on payroll tax contributions, pension, disability insurance, and health-care average and marginal payroll tax rates (both average and marginal) differ across agents. The (individual) average pension, health care and disability insurance contribution

rates are defined as  $\bar{\tau}^p(j, t, s, k)$ ,  $\bar{\tau}^h(j, t, s, k)$  and  $\bar{\tau}^d(j, t, s, k)$ , respectively. Individual tax payments in equation [10] are net of pension  $Pen(j, t, s, k)$  and disability benefits  $di$  received. Each agent's pension benefits depend on her/his pre-retirement earnings history, while health care (as part of government purchases) and disability transfers are provided on a per-capita basis to all eligible age groups. The variable  $W(j, t, s, k)$  denotes the individual gross labor income.

As already mentioned, the switch to the FairTax is accompanied by a rebate, which depends on the household's characteristics. To be precise, the rebate  $Reb_{FT}(j, t, s, k)$  in our model is the percentage,  $\pi$ , difference between the new cum-FairTax consumption tax payments determined by  $\tau_{FT}^c(t)$  and the consumption tax payments if the old (no-FairTax) nominal rate  $\tau^c(t)$  were to be maintained, i.e.,

$$[11] \quad Reb_{FT}(j, t, s, k) = \pi[\tau_{FT}^c(t) - \tau^c(t)] \cdot [c(j, t, s, 1) + \Psi KID(j, t, 1)c_K(j, t, s, 1)].$$

Note that the rebate for each income class is based on the consumption expenditures of the lowest income class ( $k = 1$ ). Consequently, the budget constraint of the household [6] in the FairTax scenario now reads

$$[12] \quad a(j+1, t+1, s, k) = [a(j, t, s, k) + I(j, t, s, k)](1+r(t)) + w(t)E(j, k)[h(j, t) - \ell(j, t, s, k)] + Reb_{FT}(j, t, s, k) - (1 + \tau_{FT}^c(t))[c(j, t, s, k) + \Psi KID(j, t, k)c_K(j, t, s, k)] - Pen(j, t, s, k) - di.$$

Given individual consumption, leisure, and asset levels of all agents, we can com-

pute aggregate variables. For example, the aggregate value of assets  $A(t + 1)$  in period  $t$  is computed from

$$[13] \quad A(t + 1) = \sum_{k=1}^3 \sum_{a=21}^{90} \underbrace{\sum_{s=23}^{45} a(a+1, t+1, s, k) N(a, t, s, k)}_{\bar{A}(a+1, t+1, k)}$$

Since households die at the beginning of each period, we have to aggregate across all agents who lived in the previous period in order to compute  $\bar{A}(a + 1, t + 1, k)$ , which we need for the calculation of bequests (see [7]). If we aggregate across agents who live in period  $t + 1$ , i.e.,

$$[14] \quad A(t + 1) = \sum_{k=1}^3 \sum_{a=21}^{90} \sum_{s=23}^{45} a(a, t + 1, s, k) \cdot N(a, t + 1, s, k),$$

assets of the arriving immigrants of period  $t + 1$  are included.

Finally, aggregate labor supply of agents in year  $t$ ,  $L(t)$ , is computed from the individual labor supplies, i.e.,

$$[15] \quad L(t) = \sum_{k=1}^3 \sum_{a=21}^{90} \sum_{s=23}^{45} E(a, k)[h(a, t) - \ell(a, t, s, k)]N(a, t, s, k).$$

### The Production Sector

The economy is populated by a large number of identical firms, the total number of which is normalized to unity. Aggregate output (net of depreciation) is produced using Cobb–Douglas production technology, i.e.,

$$[16] \quad F(K(t), L(t)) = \phi K(t)^\varepsilon L(t)^{1-\varepsilon},$$

where  $K(t)$  is aggregate capital in period  $t$ ,  $\varepsilon$  is capital's share in production, and  $\phi$  is a technology parameter. Since we posit convex capital adjustment costs following Hayashi (1982), the firms' marketable

output in year  $t$ ,  $Y(t)$ , is given by the difference between gross output and adjustment costs, i.e.,

$$[17] \quad Y(t) = F(K(t), L(t)) - 0.5\psi\Delta K(t)^2 / K(t).$$

where  $\Delta K(t)$  measures investment in year  $t$ . The implementation of adjustment costs takes into account observed lags in the investment process. These costs lead the market values of capital assets to temporarily differ from their replacement costs. The term  $\psi$  is the adjustment cost coefficient. Larger values of  $\psi$  imply higher marginal costs of new capital goods for a given rate of investment. The installation technology is linear homogeneous and shows increasing marginal cost of investment (or, symmetrically, disinvestment): faster adjustment requires a greater-than-proportional rise in adjustment costs.

Corporate taxes,  $T^k(t)$ , are given by

$$[18] \quad T^k(t) = \tau^k(t)[Y(t) - w(t)L(t) - \varepsilon(t)\Delta K(t)],$$

where  $\tau^k(t)$  and  $\varepsilon(t)$  define the corporate tax rate and the immediate write-off share of investment expenditures, respectively. Since adjustment costs are fully, and investment expenditures are partly, deductible from the tax base, arbitrage between new and existing capital implies that the latter has a price per unit of

$$[19] \quad q(t + 1) = 1 - \varepsilon(t)\tau^k(t) + [1 - \tau^k(t)]\psi\Delta K(t) / K(t).$$

Similarly, the arbitrage condition arising from profit maximization requires identical returns to financial and real investments:

$$[20] \quad r(t)q(t) = [1 - \tau^k(t)]\{F_{K(t)} + 0.5\psi(\Delta K(t) / K(t))^2\} + q(t + 1) - q(t).$$

The left side gives the return on a financial investment of amount  $q(t)$ , while the return on one unit of real capital investment is the net return to capital (which includes the marginal product of capital  $F_{k(t)}$  plus the reduction in marginal adjustment costs) and capital gains.

*The Government Sector*

The consolidated government issues new debt  $\Delta B(t)$  and collects corporate taxes and net taxes from households in order to finance general government expenditures  $G(t)$  as well as interest payments on its debt:

$$\begin{aligned}
 [21] \quad \Delta B(t) + T^k(t) & \\
 & + \sum_{k=1}^3 \sum_{a=21}^{90} \sum_{s=23}^{45} T(a, t, s, k) N(a, t, s, k) \\
 & = G(t) + r(t)B(t).
 \end{aligned}$$

With respect to public debt, we assume that the government maintains an exogenously fixed ratio of debt to output. The progressivity of the wage tax system is modeled as in Auerbach and Kotlikoff (1987). Individual marginal  $\tau^w(a, t, s, k)$  and average  $\bar{\tau}^w(a, t, s, k)$  wage tax rates consequently take the forms

$$[22] \quad \tau^w(a, t, s, k) = \beta_0 + \beta_1 W(a, t, s, k)$$

and

$$\bar{\tau}^w(a, t, s, k) = \beta_0 + \beta_1 \frac{W(a, t, s, k)}{2},$$

where the parameters  $\beta_0$  and  $\beta_1$  determine the level and progressivity of the wage tax function. Note that marginal wage tax rates rise linearly with the tax base  $W(a, t, s, k)$ . In the baseline transition, the proportional term  $\beta_0$  of the wage tax is calculated endogenously in order to balance the government budget.

$PY(t)$  defines the aggregate payroll tax base, which differs from total labor

earnings due to the ceiling on taxable wages. This ceiling is fixed at 250 percent of average annual earnings. Aggregate average social security payroll tax rates  $\hat{\tau}^p$ ,  $\hat{\tau}^h$  and  $\hat{\tau}^d$  are computed each period from the budget constraint relevant for the program in question, i.e.,

$$[23] \quad \hat{\tau}^p(t)PY(t) = PB(t),$$

$$\hat{\tau}^h(t)PY(t) = HB(t)$$

and

$$\hat{\tau}^d(t)PY(t) = DB(t),$$

where  $PB(t)$ ,  $HB(t)$  and  $DB(t)$  are total outlays of the pension, health care, and disability systems, respectively.

Due to contribution ceilings, individual pension, disability and health insurance payroll tax rates can differ from the payroll tax rate. Above the contribution ceiling, marginal social security contributions are zero and average social security contributions fall with the agent's income. To accommodate this non-convexity of the budget constraint, we assume that the highest earnings class pays the FICA Old age, survivors, and disability insurance (OASDI) payroll tax up to the ceiling, but faces no payroll taxes at the margin. The other earnings classes are assumed to face the full statutory OASDI tax rate on all earnings. However, since there is no ceiling on the health insurance (HI) FICA tax, all earnings groups are assumed to face the HI tax at the margin.

If a  $k$ -income class agent, whose parents were  $s$  years old at his birth, retires in year  $z$  at the exogenously set retirement age  $\bar{a}(z)$ , her/his pension benefits  $Pen(a, i, s, k)$  in years  $i \geq z$  when he is age  $a \geq \bar{a}(z)$  depend linearly on her/his average earnings during his working time  $\bar{W}(z, s, k)$ :

$$[24] \quad Pen(a, i, s, k) = \omega_0 + \omega_1 \times \bar{W}(z, s, k).$$

The parameters  $\omega_0$ ,  $\omega_1$  were chosen in order to approximate replacement rates

relative to individual lifetime earnings as reported in Whitehouse (2002).

General government expenditures  $G(t)$  consist of government purchases of goods and services, including educational expenditures and health outlays. Over the transition, general government purchases of goods and services are held fixed as a percent of national income. Age-specific education and disability outlays are held fixed per capita over the transition with an adjustment for technological change. Age-specific health outlays are also held fixed per capita, but are assumed to grow at twice the rate of technological change during the first 25 years of the transition. Afterwards, the age-specific levels of these outlays grow at the same rate as technological change. Note that while the outlays of the health care systems are treated as government expenditures, disability benefits are modeled as direct transfers to the households. The government's budget [21] is balanced each year by adjusting the intercept in our linear equation determining the average wage tax rate.

Next we turn to the baseline closed-economy simulation results. A detailed description of the parametrization of the model, the solution method and the key macroeconomic variables of the initial equilibrium in 2004 is given in the Appendix.

#### THE U.S. BASELINE TRANSITION PATH

In this section we discuss the baseline transition path for the closed U.S. economy, which serves as a reference case for our further analysis on the implementation of the FairTax. The baseline path assumes that all parameters of the functional forms as explained in the Appendix remain unchanged. Any transitional dynamics are, therefore, solely due to the demographic changes outlined in the first subsection of the second section and Table 1.

The baseline closed-economy simulation results are reported in the top panel of Table 4. In examining this table, note that the values of national income, the capital stock, the supply of labor, the Social Security payroll tax rate, the average wage tax, and the pre-tax wage rate are all expressed relative to their respective values in 2004.

The first column of Table 4 shows that neither America's aging nor its associated increase in payroll taxes prevents the economy from growing in absolute terms. Indeed, the model's output in 2100 is 3.84 times its 2004 value. This reflects growth over time in the supplies of both labor and capital, which expand by factors of 4.19 and 3.17, respectively, over the course of the century.

The growth of labor supply, shown in column 3, primarily reflects our assumption that each successive cohort has a higher effective time endowment, which admits greater effective labor supply by each successive cohort. Other things equal, this rising supply of effective labor means rising labor income and, therefore, more wherewithal for workers to save for retirement. The additional saving is, of course, invested, explaining the model's predicted growth in the stock of capital (see column 2).

Due to the aging of the population, the model's social security cost rate (the model's payroll tax rate) increases over the whole century. According to the development of the number of people aged 65 and older (see Table 1), the largest rise in the payroll tax rate of 55.5 [(1.68-1.08)/1.08] percent occurs between 2010 and 2030. Over the century, social security contributions more than double. Average wage tax rates, on the other hand, change very little over time. During the first years of the transition, these are slightly reduced, which reflects the dominance of increased labor supply. However, wage tax rates start to rise with the lower wage tax base due to the proceeding aging process. As a

TABLE 4  
SIMULATION RESULTS FOR THE CLOSED U.S. ECONOMY

	Year	Index of National Income	Index of Capital Stock	Index of Labor Supply	Index of Pre-Tax Wage	Capital Price	Interest Rate	Social Security Cost Index	Average Wage Tax Index	Effective FairTax Rate	FairTax Rebate/NI
Base Case	2004	1.00	1.00	1.00	1.00	1.000	0.075	1.00	1.00	0.00	0.000
	2010	1.12	1.09	1.14	0.99	1.007	0.075	1.08	0.98	0.00	0.000
	2020	1.36	1.27	1.40	0.97	1.008	0.074	1.32	0.94	0.00	0.000
	2030	1.59	1.44	1.67	0.96	0.975	0.078	1.68	1.04	0.00	0.000
	2050	2.10	1.74	2.29	0.92	0.987	0.088	1.79	1.13	0.00	0.000
	2075	2.92	2.37	3.20	0.91	0.992	0.088	1.91	1.07	0.00	0.000
	2100	3.84	3.17	4.19	0.92	0.981	0.087	2.04	1.06	0.00	0.000
FairTax	2004	1.02	1.00	1.05	0.98	1.261	0.075	0.00	0.00	0.23	0.047
	2010	1.17	1.23	1.17	1.01	1.216	0.079	0.00	0.00	0.24	0.049
	2020	1.45	1.65	1.39	1.05	1.158	0.075	0.00	0.00	0.25	0.053
	2030	1.74	2.07	1.63	1.07	1.098	0.075	0.00	0.00	0.28	0.061
	2050	2.38	2.97	2.17	1.10	1.072	0.076	0.00	0.00	0.28	0.062
	2075	3.35	4.45	2.99	1.13	1.048	0.073	0.00	0.00	0.29	0.065
	2100	4.46	6.22	3.88	1.15	1.023	0.071	0.00	0.00	0.30	0.068
Constant General Government Expenditures	2004	1.03	1.00	1.06	0.98	1.264	0.075	0.00	0.00	0.26	0.055
	2010	1.18	1.23	1.18	1.01	1.218	0.080	0.00	0.00	0.27	0.057
	2020	1.46	1.65	1.41	1.05	1.159	0.075	0.00	0.00	0.28	0.060
	2030	1.76	2.08	1.65	1.07	1.098	0.076	0.00	0.00	0.31	0.068
	2050	2.40	2.98	2.20	1.10	1.073	0.077	0.00	0.00	0.31	0.069
	2075	3.38	4.47	3.02	1.12	1.048	0.073	0.00	0.00	0.31	0.072
	2100	4.50	6.25	3.92	1.15	1.023	0.071	0.00	0.00	0.32	0.074
Constant Social Security Benefits	2004	1.02	1.00	1.05	0.98	1.280	0.075	0.00	0.00	0.21	0.040
	2010	1.17	1.24	1.17	1.02	1.231	0.077	0.00	0.00	0.21	0.041
	2020	1.46	1.69	1.39	1.06	1.166	0.073	0.00	0.00	0.22	0.044
	2030	1.75	2.14	1.62	1.09	1.104	0.073	0.00	0.00	0.24	0.050
	2050	2.40	3.10	2.16	1.11	1.076	0.074	0.00	0.00	0.24	0.051
	2075	3.39	4.67	2.97	1.15	1.050	0.070	0.00	0.00	0.24	0.052
	2100	4.51	6.55	3.85	1.17	1.024	0.068	0.00	0.00	0.25	0.055

consequence, the average tax rate in 2050 is 13 percent above its year-2004 value. In the long run, the wage tax rate slightly decreases, again reflecting the economic recovery after the peak of the aging process. Nevertheless, in 2100 the tax rate is still six percent above its initial level.

While the supplies of both labor and capital rise over time, growth in the supply of labor outpaces growth in the supply of capital thanks, in large part, to the very substantial rise in overall taxation of labor income. Consequently, capital per unit of human capital falls over time, leading to an 8.0 percent decline over the course of the century in the pre-tax wage per unit of human capital. Thus, in the base-case, no-tax reform simulation, we see a major long-run capital shortage.

However, in combination with the model's predicted rise in the payroll tax, the decline in the pre-tax wage spells a 21 percent decline in long-run after-tax take-home-pay. It also spells a major reduction in welfare, which, as we will now show, can be avoided via a switch to the FairTax.

#### THE FAIRTAX TRANSITION PATH

Table 4's second panel reports the transition path arising from eliminating the personal wage income tax, the personal capital income tax, the corporate income tax, and the payroll tax, and replacing them with a consumption tax plus a rebate. In this simulation, we set the model's 2004 FairTax rate at the 23 percent rate specified in HR25, the House bill that would implement the FairTax. As discussed in the introduction and Appendix, implementing a 23 percent FairTax in our model requires cutting discretionary spending by 18 percent as a share of national income. The alternative assumption, which we consider in the section after next, is that the scale of discretionary spending remains unchanged,

but the FairTax is implemented at an initial rate of 26 percent.

While the present simulation entails an initial 23 percent effective FairTax, the rate rises over time to 30 percent. This rise reflects, of course, the need to pay the pension and health care costs of an increasingly aged society. The development of the FairTax rebate in percent of national income is reported in the last column of Table 4. Since the rebate pays 60 percent of the increased consumption tax payments of households due to the introduction of the FairTax, the rebate increases from an initial level of 4.7 percent of national income to 6.8 percent in 2100.

As indicated above, switching to consumption taxation provides much better saving incentives. It also redistributes resources from older spenders to younger savers. We see this in the growth of the capital stock through time. As the second column in the second panel shows, the capital stock ends up dramatically higher in the long run under the FairTax than it does under the current tax system. Indeed, the capital stock in 2100 is 96.2  $[(6.22 - 3.17)/3.17]$  percent higher. While the expansion of the capital stock proceeds relatively slowly, it is noticeable even by 2010. In that year, the capital stock is 12.8 percent higher under the FairTax than would otherwise have been the case. By 2030, the capital stock is 43.7 percent higher than in the status quo transition.

The significant rise in capital formation permits two things—an expansion of U.S. output and an increase in leisure. As column 1 of Table 4 shows, output in 2100 is 16.1  $[(4.46 - 3.84)/3.84]$  percent higher thanks to the FairTax, even though the supply of labor is 7.4  $[(3.88 - 4.19)/4.19]$  percent smaller.

The increased capital formation also leads to a rise in the real wage per unit of human capital. Rather than declining by 8.0 percent by the end of the century, the real wage now rises by 17.0 percent. This

is a 25.0 percent difference in real worker remuneration. Again, the pace of change is slow, but by 2030 real wages under the FairTax are 11.5 percent higher than they would otherwise have been.

In transforming the economy's prospects from one of a capital shortage to one of capital deepening, the FairTax also reduces real interest rates, with the 2100 real interest rate ending up 160 basis points lower than in the base case.

### WELFARE EFFECTS OF SWITCHING TO THE FAIRTAX

Table 5 shows the remarkably large and highly progressive welfare gains arising for most members of current and future cohorts from the switch to the FairTax. These welfare changes are measured as the uniform percentage change in an agent's current and future consumption and leisure in the base-case economy required to achieve the same level of remaining lifetime utility as the agent enjoys under the FairTax.

Look first at the results for those born in 1920, i.e., those who are 84 at the time of the reform. The low-income members of this cohort experience a sizeable 9.4 per-

cent welfare gain. Their middle-income contemporaries experience a moderate 1.0 percent welfare gain, while their richer contemporaries experience a small 0.4 percent welfare loss.

This picture of substantial welfare gains for low-income cohort members and modest gains or small losses for middle- and high-income cohort members holds for all cohorts born before 1970. For cohorts born after 1970, we see major welfare gains not just for low-income cohort members, but for middle- and high-income members as well. But the gains to the low-income members are much higher than those of their contemporaries. Take the cohort born in 2030. Low-income members experience a 26.3 percent welfare gain, while their middle-income contemporaries experience a 12.4 percent gain, and their high-income contemporaries experience a 5.0 percent gain.

What explains the pattern of these welfare changes? The answer is in part the wealth tax component of the FairTax, in part the FairTax's preservation of the purchasing power of Social Security benefits, in part the introduction of the highly progressive rebate, in part the elimination of the highly regressive payroll tax, in part the major rise in real wages, in part the cutback on federal discretionary spending, and in part the major reduction in economic distortion arising from a tax structure that eliminates the taxation of saving and, for many households, significantly reduces the total effective tax on labor supply.<sup>6</sup>

Consider, for example, members of income class 1 who were born in 1920 and enjoy a 9.4 percent welfare gain. This gain can be traced to the fact that these households depend almost entirely on Social Security to finance their consumption. The FairTax not only preserves the

TABLE 5  
WELFARE EFFECTS OF THE FAIRTAX  
(CLOSED ECONOMY)

Birth Year	Income Class		
	1	2	3
1920	9.39	1.01	-0.40
1930	8.75	0.44	-0.54
1940	8.03	-0.11	-0.86
1950	4.71	-1.18	-1.41
1960	5.05	-0.94	-1.44
1970	7.34	0.54	-0.67
1980	9.72	2.37	0.86
1990	13.48	4.68	1.94
2000	18.18	7.43	3.02
2010	22.12	9.84	4.01
2020	24.59	11.39	4.62
2030	26.34	12.45	5.01

<sup>6</sup> Indeed, the source of the efficiency gain from the considered tax reform is the lump-sum taxation of the wealth of existing generations associated with switching to a consumption tax. The revenue from this effective lump-sum tax permits a reduction in the effective tax rate on labor income.

purchasing power of their Social Security benefits. It also provides them with the FairTax rebate. The rebate, recall, is based on demographics, not on income, i.e., all households receive the rebate regardless of income. Hence, these households are overcompensated by the FairTax and end up better off as a result.

Next, consider members of income class 1 born in 2030. What is the precise explanation for their 26.3 percent welfare gain? The answer begins with the fact that, thanks to the FairTax, they receive a pre-tax wage at the start of their work careers (roughly mid Century) that is 19.6 percent higher than it would otherwise have been. By the end of their work careers, their pre-tax wage is 25.0 percent higher than it would otherwise have been. In addition, they receive the FairTax rebate. Hence, these households pay relatively little in taxes, on net, and face an average net tax on their labor earnings of only five percent. In contrast, their average net tax under the status quo regime ranged from 19.5 percent to 23.6 percent over the course of their workspan due to their exposure to payroll (FICA) taxation. Finally, these households experience substantial efficiency gains thanks to the FairTax's complete elimination of the taxation of saving.

#### SIMULATING A SWITCH TO THE FAIRTAX THAT INVOLVES NO CUT IN THE SCALE OF DISCRETIONARY SPENDING

As explained above, the switch to the FairTax involves a cut of general government discretionary spending (general expenditures) in order to help pay for the rebate, on the one hand, and the preservation of the purchasing power of social security benefits by indexing these to the consumption tax increase, on the other hand. Of course, these two measures affect the macroeconomic outcome and the welfare of households with the introduction of the FairTax. In order to

get a better understanding of the relative magnitudes of these effects on the simulation results, we also report the findings if either general government expenditures are maintained as in the baseline path or social security benefits are not adjusted to preserve the purchasing power. Note that in both scenarios the rebate to households is again fixed at 60 percent of the consumption tax differential so that the initial effective FairTax rate deviates from the targeted rate of 23 percent.

First, consider the case where the FairTax is introduced and the level of government expenditures remains the same as in the baseline path. The macroeconomic results are shown in the third panel of Table 4. Thanks to higher government expenditures, the effective FairTax rate in 2004 is now 26 percent and increases over the century to 32 percent. Not surprisingly, the FairTax rebate is approximately 0.7 percentage points higher throughout the whole transition path. The higher tax burden leads to slightly increased labor supply, which translates into a rise in national income and the capital stock. However, the overall effects are rather small so that the transition path is mainly unchanged compared to the switch to the FairTax with the simultaneous cut in government expenditures.

The welfare effects of the FairTax without the cut in government expenditures are reported in Table 6. Obviously, welfare gains are dampened, in this case by 1.0 to 1.5 percent, and welfare losses are increased by approximately the same percentage due to the higher consumption tax payments. But this does not change our principal finding that, even without lowering government expenditures, all low-income households and future generations in all income classes are expected to experience major welfare gains by the switch to the FairTax. Given these substantial welfare improvements, welfare losses for middle- and high-income households that are currently alive are of a fairly small range.

**TABLE 6**  
WELFARE EFFECTS OF THE FAIRTAX WITH  
CONSTANT GOVERNMENT EXPENDITURES  
(CLOSED ECONOMY)

Birth Year	Income Class		
	1	2	3
1920	7.58	-0.64	-0.98
1930	7.08	-1.07	-1.05
1940	6.42	-1.62	-1.39
1950	3.33	-2.53	-2.02
1960	3.67	-2.33	-2.10
1970	5.79	-1.08	-1.51
1980	8.03	0.56	-0.15
1990	11.80	2.89	0.95
2000	16.48	5.66	2.05
2010	20.40	8.07	3.06
2020	22.88	9.65	3.68
2030	24.64	10.73	4.09

**TABLE 7**  
WELFARE EFFECTS OF THE FAIRTAX WITH  
CONSTANT SOCIAL SECURITY BENEFITS  
(CLOSED ECONOMY)

Birth Year	Income Class		
	1	2	3
1920	-1.69	-3.15	-0.59
1930	-1.90	-3.39	-0.72
1940	-3.43	-4.60	-1.18
1950	0.90	-2.34	-1.41
1960	3.71	-0.89	-1.21
1970	7.20	1.35	-0.19
1980	10.29	3.75	1.61
1990	14.50	6.43	2.87
2000	19.60	9.54	4.11
2010	23.82	12.19	5.20
2020	26.47	13.86	5.85
2030	28.41	15.04	6.29

Now we turn to the switch of the FairTax where government expenditures are again cut by 18 percent, but social security benefits are not adjusted for preserving the purchasing power. The simulation results are shown in the fourth panel of Table 4. Due to lower social security benefit payments, the initial FairTax rate is now two percentage points lower. Since over the century benefits grow to a smaller extent, the FairTax rate in 2100 is even five percentage points lower vis-à-vis the scenario with indexed benefits. This also lowers the rebate given to the households. The improved saving incentives lead to higher capital formation and national income and allow households to increase their leisure demand. These changes in the capital-labor ratio increases the pre-tax wage rate by even more compared to the FairTax scenario with adjusted social security benefits.

Welfare effects for the elderly generations in the low-income class are now substantially changed (see Table 7). Instead of large welfare gains, these generations are now expected to experience welfare losses of up to 3.4 percent for the cohorts born in 1940. This finding impressively shows how these generations are over-compensated when their benefits are adjusted to preserve purchasing power. The table furthermore indicates that the middle-income class benefits a lot from

adjusted social security benefits. Welfare losses in the high-income class are only slightly changed. It is, however, remarkable that all generations born in 1980 and later experience even higher welfare gains than in the scenario where benefits are adjusted. This, of course, reflects the more dampened increase in the effective FairTax rate and the larger rise of wages during the transition path. Given the relatively small transitional burdens, this again shows the large welfare potential of the switch to the FairTax.

## OPEN ECONOMY RESULTS

As already discussed above, the preceding integration of worldwide capital markets makes international capital flows a major determinant of domestic investment in the future. We, therefore, analyze the switch to the FairTax under the extreme assumption that the U.S. is perfectly open to international capital inflows. Tables 8 and 9 present the economic and welfare results. Table 8's index values are normalized at the year-2004 closed economy levels, i.e., the values shown are relative to the values prevailing in 2004 in the closed economy. As in our closed economy simulation, there are major economic and welfare gains from adopting the FairTax. However,

TABLE 8  
SIMULATION RESULTS FOR THE OPEN U.S. ECONOMY

Year	Index of National Income	Index of Capital Stock	Index of Labor Supply	Current Account/NI	Index of Pre-Tax Wage	Capital Price	Interest Rate	Social Security Cost Index	Average Wage Tax Index	Effective Fair Tax Rate	FairTax Rebate/NI
Base Case											
2004	1.00	1.00	1.00	0.005	1.00	0.992	0.075	1.00	1.03	0.00	0.000
2010	1.12	1.09	1.14	-0.003	0.99	1.008	0.075	1.09	0.97	0.00	0.000
2020	1.35	1.28	1.39	-0.020	0.97	1.019	0.075	1.33	0.94	0.00	0.000
2030	1.60	1.51	1.66	-0.055	0.97	1.022	0.075	1.66	1.00	0.00	0.000
2050	2.26	2.11	2.35	-0.035	0.97	1.013	0.075	1.66	1.20	0.00	0.000
2075	3.18	3.02	3.27	-0.014	0.98	0.993	0.075	1.79	1.22	0.00	0.000
2100	4.17	4.02	4.26	-0.013	0.98	0.980	0.075	1.93	1.19	0.00	0.000
FairTax											
2004	1.01	1.00	1.04	-0.031	0.99	1.299	0.075	0.00	0.00	0.23	0.047
2010	1.18	1.25	1.17	-0.009	1.02	1.228	0.075	0.00	0.00	0.24	0.048
2020	1.46	1.67	1.40	0.003	1.05	1.152	0.075	0.00	0.00	0.25	0.053
2030	1.75	2.11	1.63	-0.012	1.08	1.109	0.075	0.00	0.00	0.28	0.061
2050	2.41	3.04	2.19	0.008	1.10	1.059	0.075	0.00	0.00	0.29	0.062
2075	3.33	4.36	2.98	0.023	1.12	1.027	0.075	0.00	0.00	0.29	0.066
2100	4.31	5.75	3.82	0.016	1.13	1.011	0.075	0.00	0.00	0.29	0.070

**TABLE 9**  
WELFARE EFFECTS OF THE FAIRTAX  
(OPEN ECONOMY)

Birth Year	Income Class		
	1	2	3
1920	10.10	1.56	-0.18
1930	8.69	0.36	-0.57
1940	7.61	-0.49	-1.00
1950	4.39	-1.44	-1.60
1960	5.09	-1.00	-1.59
1970	7.58	0.67	-0.69
1980	9.84	2.54	0.98
1990	13.13	4.61	2.13
2000	16.93	6.94	3.23
2010	19.32	8.41	4.01
2020	20.39	9.05	4.37
2030	21.37	9.65	4.67

these gains are smaller than in the closed economy results.

The variable of chief interest—the pre-tax wage—rises in this simulation by 14.1 percent over the course of the century and by 15.3 percent compared to the year-2100 baseline value. This is less than the 25.0 percent rise in the closed economy simulation compared to the base case, but still sizeable.

As in the closed economy case, the rise in the pre-tax wage can be traced to higher levels of capital per worker. In the closed economy simulation, the increased saving of U.S. households, in response to the FairTax's redistributive and incentive effects, led, over time, to more capital formation. In the open economy case, the source of increased capital formation is the elimination, under the FairTax reform, of the model's assumed 30 percent effective corporate income tax. The reason is that in an open economy, capital flows in from abroad when it can get a higher return due to a reduction in corporate taxes. It continues to do so until the pre-tax return is sufficiently lowered as to make the after-tax return the same as that available abroad. This is reflected by the initial current account deficit that lasts through 2010. In the present simulation, the rise in U.S. capital formation is substantial, with the capital stock in 2100 being 43.0 percent higher than in the base-case simulation.

Although the capital stock increases smartly over time, the economy's supply of labor fails to keep pace, leaving the overall output of the economy in 2100 at roughly the same level that prevails without the FairTax. In the closed-economy switch to the FairTax, the system's effective tax rate rose from 23 percent to 30 percent. Almost the same rise occurs in the open economy simulation.

Table 9 presents open-economy welfare effects from tax reform. As in the closed economy simulation, the welfare gains accruing to old, middle-aged, young, and future poor households are remarkably large in their own right and much larger than those experienced by their middle-class and rich contemporaries. Indeed, the only major difference between Tables 9 and 5 is the slightly smaller welfare gain experienced by those born after 1990 in income class 1.

## SENSITIVITY ANALYSIS

In order to analyze the robustness of our simulation results, we finally present some sensitivity runs of our model. These runs include the abolition of capital adjustment costs ( $\psi = 0.0$ ), a lower capital share in production ( $\varepsilon = 0.25$ ), a higher intratemporal elasticity of substitution ( $\rho = 0.8$ ) and a lower leisure preference parameter ( $\alpha = 1.0$ ). The macroeconomic developments of these sensitivity runs are shown in Table 10, and the respective welfare effects of the switch to the FairTax are given in Table 11. As the simulation results indicate, the changes in the various parameters of our model of course affect the baseline transition path but leave the overall findings of the switch to the FairTax fairly unchanged.

If the installation of new capital can be done at no costs, the capital stock during the transition increases to a somewhat larger extent during the baseline transition and also during the transition path with the FairTax. The welfare gains (losses)

# Simulating the Dynamic Macroeconomic and Microeconomic Effects of the FairTax

**TABLE 10**  
SIMULATION RESULTS FOR THE SENSITIVITY ANALYSIS

	Year	Index of National Income	Index of Capital Stock	Index of Labor Supply	Index of Pre-Tax Wage	Interest Rate	Social Security Cost Index	Effective FairTax Rate
adjustment cost parameter $\psi = 0.0$								
Base Case	2004	1.00	1.10	1.00	1.00	0.071	1.00	0.00
	2050	2.10	1.85	2.30	0.91	0.088	1.79	0.00
	2100	3.83	3.40	4.20	0.91	0.087	2.05	0.00
FairTax	2004	1.06	1.09	1.09	0.97	0.108	0.00	0.26
	2050	2.43	3.64	2.14	1.14	0.074	0.00	0.27
	2100	4.49	7.16	3.85	1.17	0.070	0.00	0.29
capital share in production $\varepsilon = 0.25$								
Base Case	2004	0.96	1.00	1.03	1.00	0.075	0.98	0.00
	2050	2.00	1.50	2.39	0.90	0.082	1.77	0.00
	2100	3.63	2.69	4.38	0.89	0.084	2.02	0.00
FairTax	2004	0.99	1.00	1.08	0.99	0.075	0.00	0.24
	2050	2.20	2.55	2.29	1.03	0.070	0.00	0.29
	2100	4.09	5.17	4.13	1.06	0.065	0.00	0.31
intra-temporal elasticity of substitution $\rho = 0.8$								
Base Case	2004	0.97	1.00	0.97	1.00	0.075	1.02	0.00
	2050	2.09	2.07	2.13	0.98	0.073	1.76	0.00
	2100	3.82	3.79	3.90	0.98	0.073	2.02	0.00
FairTax	2004	1.00	1.00	1.04	0.98	0.075	0.00	0.22
	2050	2.49	3.51	2.19	1.14	0.067	0.00	0.24
	2100	4.75	7.50	3.97	1.20	0.062	0.00	0.25
leisure preference parameter $\alpha = 1.0$								
Base Case	2004	1.10	1.00	1.10	1.00	0.075	0.95	0.00
	2050	2.35	1.92	2.47	0.95	0.089	1.66	0.00
	2100	4.31	3.58	4.50	0.96	0.087	1.90	0.00
FairTax	2004	1.12	1.00	1.15	0.99	0.075	0.00	0.21
	2050	2.64	3.19	2.36	1.13	0.079	0.00	0.26
	2100	4.98	6.77	4.21	1.19	0.073	0.00	0.27

**TABLE 11**  
WELFARE EFFECTS OF THE FAIRTAX IN THE SENSITIVITY ANALYSIS

Birth Year	Income Class			Income Class		
	1	2	3	1	2	3
$\psi = 0.0$						
1920	3.32	-3.58	-2.47	9.23	0.84	-0.60
1960	5.15	-1.29	-1.93	4.92	-1.12	-1.60
2000	22.57	10.37	4.46	17.09	6.56	2.68
2030	30.17	14.95	6.16	23.78	10.62	4.28
$\rho = 0.8$						
$\alpha = 1.0$						
1920	4.86	1.30	-1.18	11.23	2.37	-0.18
1960	3.45	-0.33	-0.43	4.55	-0.79	-1.11
2000	10.31	5.23	4.77	15.68	6.57	3.39
2030	14.77	8.92	7.25	23.10	11.31	5.41

of the switch to the FairTax are slightly dampened (increased) for elderly people, which is due to a higher initial FairTax rate. However, future generations again experience large benefits, which are even higher than in our basic calibration.

Reducing the leisure preference parameter translates into increased labor supply and, therefore, higher capital formation and national income during the baseline transition. The changed capital–labor ratio leads to a dampened decrease in the wage rate. Again, the switch to the FairTax yields very similar results than with our basic calibration.

Lowering the capital share in production of course increases labor supply and dampens capital accumulation during the baseline. Wage rates are, therefore, reduced to a larger extent during the base case and the interest rate increase is dampened. The switch to the FairTax again boosts the capital stock, and welfare effects remain almost identical to the findings with the basic calibration.

Finally, doubling the value of the intra-temporal elasticity of substitution reveals the largest changes of our results. On the one hand, this refers to the development of the capital–labor ratio in the baseline transition. Since labor supply and the capital stock evolve almost identically, factor prices are fairly unchanged during the transition. Consequently, the wage rate is only two percent below its initial value and the interest rate is now reduced by 20 basis points. On the other hand, despite similar macroeconomic developments of the switch to the FairTax, welfare effects are much more dampened for the low-income class and increased for the high-income class compared to the basic calibration. Nevertheless, the welfare gains that can be achieved with the switch to the FairTax are still large compared to the welfare losses experienced by some initially elderly generations.

Obviously, the sensitivity analysis in this section shows that the findings of the switch to the FairTax are very robust to the parameter choices in our model. This finding supports the FairTax as a beneficial alternative given the future economic and fiscal burdens expected from the aging process of the U.S. population.

## CONCLUSION

The aging of the U.S. coupled with its high and growing pension and old age health care benefits augers much higher payroll taxes, with potentially damaging effects on the macroeconomy. This prognosis is supported by our base-case simulation, which generates more than a doubling of the payroll tax rate as well as a modest, but significant, long-run capital shortage. This crowding out of capital gradually reduces real wages per unit of human capital by eight percent. In combination with the long-run 12 percentage point rise in the payroll tax, the model's predicted long-run reduction in worker take-home-pay is 21 percent.

The FairTax offers an alternative to this dismal economic future. The FairTax proposes to replace the federal payroll tax, personal income tax, corporate income tax, and estate tax (not modeled here) with a federal retail sales tax plus a rebate. In switching from taxing income to taxing consumption and adding a highly progressive rebate, the FairTax introduces many progressive elements into our fiscal system, removes one very regressive element (the payroll tax), and provides much better incentives to work and save.

According to our model, switching to the FairTax would raise long-run capital intensity, raising long-run real wages by 25 percent compared to the base-case alternative. The reform also generates major welfare gains for the poorest members of society, including

those now retired and those yet to be born. The remarkable finding of this study is how small are the transition costs associated with this reform. Yes, some initial high- and middle-income households are made worse off, but their welfare losses are minor compared with the gains available to future generations, particularly the poorest members of future generations.

The economic and welfare gains from switching to the FairTax are somewhat smaller if, as we feel is closest to the truth, one models the U.S. economy as fully open to international capital flows. But these gains are, nonetheless, large and very significant. The sensitivity analysis showed that the large beneficial welfare effects of the switch to the FairTax are robust to the model's parameter changes.

While our model is highly stylized, it suggests that the FairTax offers a real opportunity to improve the U.S. economy's performance and the well-being of the vast majority of citizens. The winners from this reform, primarily those who are least well off, experience very major gains, and the losers experience only minor losses.

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### REFERENCES

Altig, David, Alan J. Auerbach, Laurence J. Kotlikoff, Kent A. Smetters, and Jan Walliser. "Simulating Fundamental Tax Reform in the United States." *American Economic Review* 91 No. 3 (June, 2001): 574–95.

Auerbach, Alan J., and Laurence J. Kotlikoff. "An Examination of Empirical Tests of Social Security and Savings." In *Social Policy Evaluation: An Economic Perspective*, edited by Elhanan Helpman, Assaf Razin, and Efraim

Sadka, 161–79. New York: Academic Press, 1983.

Auerbach, Alan J., and Laurence J. Kotlikoff. *Dynamic Fiscal Policy*. Cambridge, England: Cambridge University Press, 1987.

Bachman, Paul, Jonathan Haughton, Laurence J. Kotlikoff, Alfonso Sanchez-Penalver, and David G. Tuerck. "Taxing Sales Under the Fair Tax: What Rate Works?" NBER Working Paper No. 12732. Cambridge, MA: National Bureau of Economic Research, 2006.

Bloendal, Sveinbjörn, and Stefano Scarpetta. "The Retirement Decision in OECD Countries." OECD Economics Department Working Paper No. 202. Paris: Organisation for Economic Co-operation and Development, 1998.

Bohn, Henning. "Social Security and Demographic Uncertainty: The Risk Sharing Properties of Alternative Policies." In *Risk Aspects of Investment Based Social Security Reform*, edited by John Campbell and Martin Feldstein, 203–41. Chicago: University of Chicago Press, 2001.

Cooley, Thomas F., and Jorge Soares. "A Positive Theory of Social Security Based on Reputation." *Journal of Political Economy* 107 No. 1 (February, 1999a): 135–60.

Cooley, Thomas F., and Jorge Soares. "Privatizing Social Security." *Review of Economic Dynamics* 2 No. 3 (July, 1999b): 731–55.

De Nardi, Mariacristina, Selahattin İmrohoroğlu, and Thomas J. Sargent. "Projected U.S. Demographics and Social Security." *Review of Economic Dynamics* 2 No. 3 (July, 1999): 575–615.

European Commission. *Statistical Annex to European Economy, Spring 2005*. [http://europa.eu.int/comm/economy\\_finance/publications/european\\_economy/statisticalannex\\_en.htm](http://europa.eu.int/comm/economy_finance/publications/european_economy/statisticalannex_en.htm). July 1, 2005.

Fehr, Hans, and Christian Habermann. "Risk Sharing and Efficiency Implications of Government Pension Arrangements."

- CESifo Working Paper No. 1568. Munich: Center for Economic Studies & Ifo Institute for Economic Research, 2005.
- Fehr, Hans, Gitta Halder, Sabine Jokisch, and Laurence J. Kotlikoff.  
 "A Simulation Model for the Demographic Transition in the OECD—Data Requirements, Model Structure and Calibration." Wuerzburg Economic Papers No. 45. Wuerzburg: University of Wuerzburg, 2003.
- Fehr, Hans, Sabine Jokisch, and Laurence J. Kotlikoff.  
 "Fertility, Mortality, and the Developed World's Demographic Transition." CESifo Working Paper No. 1326. Munich: Center for Economic Studies & Ifo Institute for Economic Research, 2004a.
- Fehr, Hans, Sabine Jokisch, and Laurence J. Kotlikoff.  
 "The Role of Immigration in Dealing with the Developed World's Demographic Transition." *Finanzarchiv* 60 No. 3 (September, 2004b): 296–324.
- Fehr, Hans, Sabine Jokisch, and Laurence J. Kotlikoff.  
 "The Developed World's Demographic Transition—The Roles of Capital Flows, Immigration, and Policy." In *Social Security Reform—Financial and Political Issues in International Perspective*, edited by Robin Brooks and Assaf Razin, 11–43. Cambridge: Cambridge University Press, 2005a.
- Fehr, Hans, Sabine Jokisch, and Laurence J. Kotlikoff.  
 "Will China Eat Our Lunch or Take Us Out to Dinner? Simulating the Transition Paths of the U.S., EU, Japan, and China." NBER Working Paper No. 11668. Cambridge, MA: National Bureau of Economic Research, 2005b.
- Feldstein, Martin S.  
 "Social Security, Induced Retirement, and Aggregate Capital Accumulation." *Journal of Political Economy* 82 No. 5 (September/October, 1974): 905–26.
- Feldstein, Martin S., and Charles Horioka.  
 "Domestic Saving and International Capital Flows." *Economic Journal* 90 No. 358 (June, 1980): 314–29.
- Gale, William G.  
 "The National Retail Sales Tax: What Would the Rate Have to Be?" Tax Notes: 889–91. Washington, D.C.: The Brookings Institution, May 16, 2005.
- Gokhale, Jagadeesh, Laurence J. Kotlikoff, and Alexi Sluchynsky.  
 "Does It Pay to Work?" NBER Working Paper No. 9096. Cambridge, MA: National Bureau of Economic Research, 2002.
- Hayashi, Fumio.  
 "Tobin's Marginal  $q$  and Average  $q$ : A Neoclassical Interpretation." *Econometrica* 50 No. 1 (January, 1982): 213–24.
- Heckman, James J., Lance Lochner, and Christopher Taber.  
 "Tax Policy and Human Capital Formation." *American Economic Review* 88 No. 2 (May, 1998): 293–97.
- Huang, He, Selahattin Imrohoroglu, and T. Sargent.  
 "Two Computational Experiments to Fund Social Security." *Macroeconomic Dynamics* 1 No. 1 (February, 1997): 7–44.
- Hubbard, Glenn R., and Kenneth L. Judd.  
 "Social Security and Individual Welfare: Precautionary Saving, Borrowing Constraints, and the Payroll Tax." *American Economic Review* 77 No. 4 (September, 1987): 630–46.
- Huggett, Mark, and Gustavo Ventura.  
 "On the Distributional Effects of Social Security Reform." *Review of Economic Dynamics* 2 No. 3 (July, 1999): 498–531.
- Imrohoroglu, Ayşe, Selahattin Imrohoroglu, and Douglas H. Joines.  
 "A Life Cycle Analysis of Social Security." *Economic Theory* 6 No. 1 (June, 1995): 83–114.
- Imrohoroglu, Ayşe, Selahattin Imrohoroglu, and Douglas H. Joines.  
 "Social Security in an Overlapping Generations Economy with Land." *Review of Economic Dynamics* 2 No. 3 (July, 1999): 638–65.
- Jokisch, Sabine.  
*The Developed World's Demographic Transition: Implications for Fiscal Policy and the International Macroeconomy*. Tübingen: Mohr Siebeck, 2006.

- Kotlikoff, Laurence J.  
 "Social Security and Equilibrium Capital Intensity." *Quarterly Journal of Economics* 93 No. 2 (May, 1979): 233–54.
- Kotlikoff, Laurence J.  
 "Privatizing Social Security: How It Works and Why It Matters." In *Tax Policy and the Economy*, Vol. 10, edited by James M. Poterba, 1–32. Cambridge, MA: MIT Press, 1996.
- Kotlikoff, Laurence J., and David Rapson.  
 "Would the FairTax Raise or Lower Marginal and Average Taxes?" NBER Working Paper No. 11831. Cambridge, MA: National Bureau of Economic Research, 2005.
- Kotlikoff, Laurence J., Kent Smetters, and Jan Walliser.  
 "The Economic Impact of Privatizing Social Security." In *Redesigning Social Security*, edited by Horst Siebert, 327–48. Tübingen: J.C.B. Mohr (Paul Siebeck), 1998a.
- Kotlikoff, Laurence J., Kent Smetters, and Jan Walliser.  
 "Social Security: Privatization and Progressivity." *American Economic Review* 88 No. 2 (May, 1998b): 137–41.
- Kotlikoff, Laurence J., Kent Smetters, and Jan Walliser.  
 "Privatizing Social Security in the U.S.: Comparing the Options." *Review of Economic Dynamics* 2 No. 3 (July, 1999): 532–74.
- Kotlikoff, Laurence J., Kent Smetters, and Jan Walliser.  
 "Finding a Way out of America's Demographic Dilemma." NBER Working Paper No. 8258. Cambridge, MA: National Bureau of Economic Research, 2001.
- Kotlikoff, Laurence J., Kent Smetters, and Jan Walliser.  
 "Distributional Effects in a General Equilibrium Analysis of Social Security." In *The Distributional Aspects of Social Security and Social Security Reform*, edited by Martin S. Feldstein and Jeffrey B. Liebman, 327–61. Chicago: University of Chicago Press, 2002.
- Krusell, Per, Vincenzo Quadrini, and José-Victor Ríos-Rull.  
 "Are Consumption Taxes Really Better Than Income Taxes?" *Journal of Monetary Economics* 37 No. 3 (June, 1996): 475–504.
- Mc Morrow, Kieran, and Werner Roeger.  
*The Economic and Financial Market Consequences of Global Ageing*. Berlin: Springer, 2004.
- Nishiyama, Shinichi, and Kent Smetters.  
 "Consumption Taxes, Risk Sharing and Economic Efficiency." *Journal of Political Economy* 113 No. 5 (October, 2005): 1088–115.
- Organisation for Economic Co-operation and Development (OECD).  
*Education at a Glance: OECD Indicators 2003*. Paris: Organisation for Economic Co-operation and Development, 2003.
- Raffelhüschen, Bernd.  
*Anreizwirkungen des Systems der sozialen Alterssicherung. Eine dynamische Simulationsanalyse*. Frankfurt a.M.: Peter Lang, 1989.
- Raffelhüschen, Bernd.  
 "Funding Social Security Through Pareto Optimal Conversion Policies." *Journal of Economics Suppl.* 7 (1993): 105–31.
- Seidman, Laurence S.  
 "A Phase-Down of Social Security: The Transition in a Life Cycle Growth Model." *National Tax Journal* 39 No. 1 (March, 1986): 97–107.
- Smetters, Kent, and Jan Walliser.  
 "Opting Out of Social Security." *Journal of Public Economics* 88 No. 7–8 (July, 2004): 1295–306.
- Summers, Lawrence H.  
 "Capital Taxation and Accumulation in a Life-Cycle Growth Model." *American Economic Review* 71 No. 4 (September, 1981): 533–44.
- United Nations Population Division (UNPD).  
*World Population Prospects: The 2002 Revision*. <http://esa.un.org/unpp/>. June 11, 2003.
- United Nations Population Division (UNPD).  
*World Population Prospects: The 2004 Revision*. <http://esa.un.org/unpp/>. June 29, 2005.
- Whitehouse, Edward.  
 "Pension Systems in 15 Countries Compared: The Value of Entitlements." Discussion Paper 02/04. Sydney: Centre for Pensions and Superannuation, 2002.

APPENDIX

This Appendix discusses in detail the parametrization of our simulation model described in the second section and explains the method applied to solve the simulation model. Afterwards, the key macroeconomic variables in the initial equilibrium are presented.

*Parametrization of the Model*

To simulate the model we need, of course, to specify preference, technology, and policy parameters. Table 2 reports these values, which, in the case of preference and technology parameters, are mostly taken from Kotlikoff, Smetters and Walliser (2001). We adopt the OECD equivalence scale of 0.5 for children’s consumption. Technological growth is assumed to be one percent.

The multi-factor technology coefficient in the U.S. Cobb–Douglas function was set to generate a U.S. marginal product of labor of 1.0 in the initial year 2004. The time–preference rate was set to match the model’s 2004 ratio of private consumption to national income to the U.S. ratio reported in European Commission (2005).

The model’s debt level of 60 percent was chosen in close accordance to the year–2004 level. The maximum age of retirement is taken

from Bloendal and Scarpetta (1998). We set the excise tax rate, personal capital income tax rate, corporate income tax rate, and expensing rate in line with the structure of indirect and direct tax revenues reported in European Commission (2005).

Our wage tax system is assumed to be progressive, with the parameters of this tax system set so as to generate what seem to be realistic averages and marginal tax rates, which are reported below.

We set the marginal effective corporate income tax rate equal to 30 percent. To ensure the correct ratio of corporate income tax revenue to national income, we also provide an inframarginal lump–sum transfer of corporate income tax revenues to households each year. This transfer is provided in proportion to each household’s asset holdings.

In simulating the FairTax, we set the rebate  $\pi$  to 60 percent, which is provided to all agents regardless of income, in order to yield a 23 percent effective FairTax rate in our FairTax closed as well as open economy simulations.

We assume uniform Medicare expenditures by age for those 65 and older and uniform disability benefit payments for those 20 to 65. Total social insurance outlays for pensions, disability, and health, measured as a share of national income, are set to accord with the values of these

TABLE 2  
PARAMETER VALUES OF THE MODEL

	Symbol	Value
Utility Function		
Time preference rate	$\theta$	0.01
Intertemporal elasticity of substitution	$\gamma$	0.25
Intratemporal elasticity of substitution	$\rho$	0.40
Leisure preference parameter	$\alpha$	1.50
Production Function		
Technology level	$\phi$	1.01
Capital share in production	$\varepsilon$	0.30
Adjustment cost parameter	$\psi$	10.0
Technical progress	$\lambda$	0.01
Policy Parameters		
Excise tax rate (in %)	$\tau$	10.2
Personal capital income tax rate (in %)	$\tau$	11.0
Marginal corporate tax rate (in %)	$\tau^c$	30.0
Expensing rate (in %)	$\varepsilon$	0.0
Debt (in % of national income)	$B/Y$	60.0
Age of retirement	$\bar{a}$	63

totals reported in European Commission (2005). We calculated a U.S. age–wealth profile using the 1998 Survey of Consumer Finances. The model’s initial asset level was set to generate a 2004 capital–output ratio of 2.7.

### *Solving the Model*

Initial (year 2004) asset holdings, the ratio of government debt to national income, and the inter– and intragenerational distribution of assets constitute the initial conditions needed to solve for the perfect foresight general equilibrium transition path of the economy. The algorithm we use to solve the model employs Gauss–Seidel iteration and the assumption that the economy has achieved a steady state by the year 2300. This assumption provides, in effect, terminal conditions to help solve for the economy’s perfect foresight transition path.

Specifically, our algorithm starts with initial guesses of the aggregate demands for capital stocks and labor supplies for the post–2004 years of the transition. Next we compute from the profit maximizing factor demand conditions the paths of wage rates and interest rates consistent with these guessed factor demands. Step three uses these pre–tax factor prices to determine aggregate household supplies of assets and labor in each transition year.

The first–order conditions and lifetime budget constraints determining household labor and asset supplies are complex and certainly do not omit of closed form solutions. Part of this complexity arises because of the progressive nature of our assumed wage tax structures, which means that marginal tax rates are themselves endogenous and need to be determined jointly with life–cycle consumption, saving, and labor supply decisions. This is also done using Gauss–Seidel iteration. We refer to this as “inter–loop” convergence. As indicated momentarily, we also use Gauss–Seidel iteration to determine the time path of the economy’s macroeconomic variables. We refer to this iteration on macro variables as “outer–loop” convergence.

The next step in our overall solution algorithm uses the annual revenues and Social Security benefit payments implied by these house-

hold decisions to update annual tax rates/tax parameters. We also update the model’s time path of government debt. These updates are based on equations [21] and [23].

Aggregating individual labor supplies in each year provides a new time path of aggregate labor supply. The corresponding new time path of the household sector’s supply of capital is determined by subtracting government debt from total household sector asset supply in each future year. Next, we form a weighted average of the initial guessed time paths of capital and labor and the aggregate supplies of these factors derived from household behavior. These weighted averages for each year are then used as the new guess for the aggregate demand for capital and labor. The algorithm continues in this manner until it converges to many decimal places.

As indicated, we give our economy 300 years to reach a steady state. In fact, our model reaches a steady state to many decimal places decades prior to year 300. It also converges very tightly around the equilibrium transition path.

We can run our model as either a closed economy or an open economy. In the open economy simulation presented below, we peg the economy’s post–corporate tax rate of return at the year–2004 value in our closed economy simulation.

To accommodate the FairTax’s insulation of the real purchasing power of Social Security benefits, we raise the size of these benefits by 30 percent, which is the FairTax retail sales tax rate. In implementing the FairTax, we also impose an 18 percent permanent cut in government purchases of goods and services starting in our 2004 base year, which helps to pay the FairTax rebate to households. This may seem like a substantial reduction in discretionary federal spending, but one needs to bear in mind that such spending has increased by 22.2 percent since 2000 measured as a share of national income.

### *Initial Equilibrium in 2004*

Table 3 reports key macroeconomic variables in 2004 in the U.S. There is very close

accordance between actual and computed values of private consumption and government purchases measured as a share of national income. The reported ratio of educational expenditures to national income is also targeted well by our model (see OECD (2003, p. 178)). The model also closely matches the share of national income received in the form of social contributions as reported in European Commission (2005). On the other

hand, our model's pension Old age and survivors insurance (OASI) contribution rate is significantly lower than the official rate. This appears to reflect the limitations of having only three earnings groups within each cohort—a limitation arising from computational considerations. Finally, the model does a reasonably good job generating the right ratios of direct and indirect taxes to national income.

**TABLE 3**  
THE YEAR 2004 OF THE BASELINE PATH<sup>a</sup>

	Model	Official <sup>b</sup>
National Income		
Private consumption	78.8	79.3
Government purchases of goods and services	17.4	17.4
General public expenditures	9.6	–
Aggregate education outlays	5.9	5.9
Aggregate health benefits	1.9	2.5
Government Indicators		
Social contributions received	8.0	7.9
Aggregate pension benefits	5.2	5.7
Aggregate health benefits	1.9	2.5
Aggregate disability benefits	0.9	0.9
Pension contribution rate <sup>c</sup>	8.1	10.6
Health-care contribution rate <sup>c</sup>	2.7	2.9
Disability-insurance contribution rate <sup>c</sup>	1.4	1.9
Interest payment on public debt <sup>c</sup>	4.5	3.0
Tax revenues <sup>c</sup>	18.7	20.6
Direct taxes	10.7	12.5
Personal income taxes	7.6	9.5
Wage taxes	4.7	–
Capital taxes	2.9	–
Corporate income taxes	3.1	3.0
Indirect taxes	8.0	8.1
Wage tax rates <sup>c</sup>		
Average	6.9	–
Marginal	12.4	–
Capital-output ratio	2.7	–
Capital-labor ratio	3.9	–
Interest rate <sup>c</sup>	7.5	–

<sup>a</sup>In percent of national income if not stated differently.

<sup>b</sup>European Commission (2005).

<sup>c</sup>In percent.